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ҚАЗАҚСТАН РЕСПУБЛИКАСЫ  
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әл-Фараби атындағы Қазақ ұлттық университетінің

# Х А Б А Р Л А Р Ы

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## ИЗВЕСТИЯ

НАЦИОНАЛЬНОЙ АКАДЕМИИ НАУК  
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## NEWS

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### THE ROLE OF RESONANCES IN THE CAPTURE OF ${}^8\text{Li}(p,\gamma){}^9\text{Be}$ ON THE REACTION RATE OF THE RELEVANT ASTROPHYSICAL SYNTHESIS OF ${}^9\text{Be}$

**Abstract:** the total cross sections of the radiative proton capture on  ${}^8\text{Li}$  at astrophysical energies are considered in the framework of the modified potential cluster model with forbidden states, with the classification of the orbital cluster states according to Young diagrams. The recalculation of the total cross sections for  ${}^9\text{Be}(\gamma,p){}^8\text{Li}$  photodisintegration is used as experimental data. Parameters for Gaussian partial potentials were obtained for description the  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  capture at astrophysical energies. It is evident that the processes of two-body radiative capture connected with them by the detailed balancing principle lead to the synthesis of  ${}^9\text{Be}$  and require the corresponding estimation contextually in the astrophysical supplements. Meanwhile, it should be noted that the first three reactions have the Coulomb barrier in channels  $p{}^8\text{Li}$ ,  $d{}^7\text{Li}$  and  $t{}^6\text{Li}$  lower than in  ${}^3\text{He}{}^6\text{He}$  along with  ${}^4\text{He}{}^5\text{He}$  channels, namely, in the ratio of 3:4. The cross section of  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  is hard to obtain directly due to low  ${}^8\text{Li}$  beam intensity and the small cross section at astrophysical energies. In addition, the difficulty of studying the reaction of  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  also lies in the fact that the direct experimental measurement of cross sections is practically impossible due to the very short half-life of  ${}^8\text{Li}$  – 838 ms. However, as in the case of the neutron capture on  ${}^8\text{Li}$ , some indirect methods of extracting direct capture cross sections can be used with the help of the radiative capture model and spectroscopic factor. The data obtained from the  ${}^9\text{Be}(\gamma,p){}^8\text{Li}$  photodisintegration process according to the detailed balancing principle are used for the experimental data of the  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  capture. It is possible to reproduce the available data on cross sections at the energies up to 7.0 MeV. Astrophysical  $S$ -factors and reaction rates  $\langle\sigma v\rangle$  are calculated at the temperature range of 0.01 to 10  $T_9$ . It is shown that the reaction rate is significantly affected by the resonances in the  $p{}^8\text{Li}$  scattering channel, and, especially by the first  $1/2^-$  resonance at 87 keV. The analytical parametrization is performed for the calculated reaction rate  $\langle\sigma v\rangle$ .

**Key words:** nuclear astrophysics; primordial nucleosynthesis; thermal and astrophysical energies;  $p{}^8\text{Li}$  cluster system; radiative capture; total cross section.

**Introduction.** The study of the formation mechanisms of  ${}^9\text{Be}$  directly concerns the problem of the overlap of the  $A = 8$  mass gap and the synthesis of heavier elements in the early Universe, as well as the  $r$ -process nucleosynthesis in supernovae (see, for example, [1,2]). In the present time, it is considered that  ${}^9\text{Be}$  is formed as a result of a two-stage process: the radiative capture of alpha particles  $\alpha(\alpha, \square){}^8\text{Be}$ , leading to the synthesis of the short-half-life isotope  ${}^8\text{Be}$  ( $t_{1/2} = 6.7 \times 10^{-17}\text{s}$ ), and radiative neutron capture  ${}^8\text{Be}(n, \square){}^9\text{Be}$  [2,3]. In addition, there is the more difficult process of the direct three-particle capture  $\alpha\alpha n \rightarrow \square{}^9\text{Be}$ , (see, for example, [4–8]).

Simultaneously, in [8], different binary channels of disintegration of  ${}^9\text{Be}$ , namely,  ${}^9\text{Be}(\square, p){}^8\text{Li}$ ,  ${}^9\text{Be}(\square, d){}^7\text{Li}$ ,  ${}^9\text{Be}(\square, t){}^6\text{Li}$  and also  ${}^9\text{Be}(\square, {}^3\text{He}){}^6\text{He}$ , were experimentally studied. It is evident that the processes of two-body radiative capture connected with them by the detailed balancing principle lead to the synthesis of  ${}^9\text{Be}$  and require the corresponding estimation contextually in the astrophysical supplements. Meanwhile, it should be noted that the first three reactions have the Coulomb barrier in channels  $p{}^8\text{Li}$ ,  $d{}^7\text{Li}$  and  $t{}^6\text{Li}$  lower than in  ${}^3\text{He}{}^6\text{He}$  along with  ${}^4\text{He}{}^5\text{He}$  channels, namely, in the ratio of 3:4.

The cross section of  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  is hard to obtain directly due to low  ${}^8\text{Li}$  beam intensity and the small cross section at astrophysical energies. In addition, the difficulty of studying the reaction of  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  also

lies in the fact that the direct experimental measurement of cross sections is practically impossible due to the very short half-life of  ${}^8\text{Li}$  – 838 ms [9]. However, as in the case of the neutron capture on  ${}^8\text{Li}$  [10], some indirect methods of extracting direct capture cross sections can be used with the help of the radiative capture model and spectroscopic factor [9,11].

The  $p{}^8\text{Li} \rightarrow {}^9\text{Be}\gamma$  reaction presents significant astrophysical interest because it is included in the list of processes of primordial nucleosynthesis of the Universe [12]. However, its experimental investigation in the astrophysical range has so far been insufficient. Intrinsically, there is only one work [13] where the astrophysical range is considered. In [14], it is also added, where measurements were carried out at higher energies. However, these works were published in the 1960s and we do not currently possess more modern experimental studies of the total cross sections of the considered reaction [15]. This is in spite of the fact that studies of spectra  ${}^9\text{Be}$  in the  $p{}^8\text{Li}$  channel are still continuing [16]. In addition, the available and considered further theoretical results differ so greatly that it is difficult to draw certain conclusions regarding the rate of this reaction. Furthermore, these calculations do not take into account the existence of resonances in the  $p{}^8\text{Li}$  system at low energies [16].

In the present study, we consider the reaction of the proton capture on  ${}^8\text{Li}$  in the frame of the modified potential cluster model (MPCM) [17] and define how the criteria of this model allow us to correctly describe total cross sections and the astrophysical  $S$ -factor at astrophysical energies. The energy range of 10 keV to 7.0 MeV is considered but only taking into account the structure of resonances up to 2.0 MeV, as discussed previously [16]. The rate of the reaction is calculated at the temperature range of 0.01 to 10  $T_9$ . The analysis of the influence of the location and magnitude of resonances to the value and shape of the reaction rate is presented.

**Materials and methods.** *Model and calculation methods.* Further we use well-known formulas for total cross sections and matrix elements of E1 transition operators [18] ( $S_i = S_f = S$ )

$$\sigma_c(NJ, J_f) = \frac{8\pi K e^2}{\hbar^2 q^3} \frac{\mu \cdot A_j^2(NJ, K)}{(2S_1 + 1)(2S_2 + 1) J[(2J + 1)!!]^2} \sum_{L_i, J_i} P_j^2(NJ, J_f, J_i) I_j^2(J_f, J_i), \quad (1)$$

where matrix elements of  $EJ$  – transitions have a form

$$P_j^2(EJ, J_f, J_i) = \delta_{S_i, S_f} [(2J + 1)(2L_i + 1)(2J_i + 1)(2J_f + 1)] (L_i 0 J 0 | L_f 0)^2 \left\{ \begin{matrix} L_i & S & J_i \\ J_f & J & L_f \end{matrix} \right\}^2$$

$$A_j(EJ, K) = K^j \mu^j \left( \frac{Z_1}{m_1^j} + (-1)^j \frac{Z_2}{m_2^j} \right), \quad I_j(J_f, J_i) = \langle \chi_f | r^j | \chi_i \rangle \quad (2)$$

Here  $S_i, S_f, L_i, L_f, J_i, J_f$  – are total spins and moments of input ( $i$ ) and output ( $f$ ) channel particles,  $m_1, m_2, Z_1, Z_2$  are masses and charges of input channel particles,  $I_j$  is the integral over wave functions of the initial  $\chi_i$  and final  $\chi_f$  states, as relative motion functions of clusters with intercluster distance  $r$ ,  $\mu$  – reduced mass.

For the spin part of the magnetic process  $M1(S)$  at  $J = 1$ , the following expression is obtained in the model used ( $S_i = S_f = S, L_i = L_f = L$ )

$$P_1^2(M1, J_f, J_i) = \delta_{S_i, S_f} \delta_{L_i, L_f} [S(S + 1)(2S + 1)(2J_i + 1)(2J_f + 1)] \left\{ \begin{matrix} S & L & J_i \\ J_f & 1 & S \end{matrix} \right\}^2,$$

$$A_1(M1, K) = \frac{\hbar K}{m_0 c} \sqrt{3} \left[ \mu_1 \frac{m_2}{m} - \mu_2 \frac{m_1}{m} \right], \quad I_1(J_f, J_i) = \langle \chi_f | r^{j-1} | \chi_i \rangle. \quad (3)$$

Here,  $m$  is the mass of the nucleus,  $\mu_1, \mu_2$  are magnetic moments of the clusters, and the remaining notation, are given as in the previous expression.

Constant  $\hbar^2/m_0$  is equal to 41.4686 MeV fm<sup>2</sup>, where  $m_0$  is the atomic mass unit (amu). The Coulomb potential at zero Coulomb radius  $R_{\text{coul}} = 0$  is written in the form  $V_{\text{coul}} = 1.439975 \cdot Z_1 Z_2 / r$ , where  $r$  is the relative distance between particles of the initial channel in fm and  $Z$  are charges of particles in the elementary charge “ $e$ ” units. Furthermore, the magnetic moment of proton  $\mu_p = 2.792847\mu_0$  and  ${}^8\text{Li}$  nucleus  $\mu({}^8\text{Li}) = 1.65356\mu_0$  [18], where  $\mu_0$  is the nuclear magneton.

**Criteria of the potential construction.** The potentials of resonance waves are constructed in order to correctly describe the location of resonance  $E_r$  and its width  $\Gamma_{\text{c.m.}}$ , therefore their parameters are obtained quite unambiguously. GS potentials will be constructed in such a form that allows one to correctly describe the channel binding energy, the charge radius of  ${}^9\text{Be}$  and its asymptotic constant in the  $p{}^8\text{Li}$  channel. Since, all known values of the asymptotic normalization coefficient (ANC) and the spectroscopic factor  $S_f$ , according to which the asymptotic constant (AC) is obtained, have enough large error. The GS potentials also can have few options with different parameters of width. However, at the given values of AC and

binding energy, its parameters are constructed absolutely unambiguously.

The spectroscopic factor  $S_f$  of the GS and  $A_{NC}$  ANC are connected by the next way [19]:

$$A_{NC}^2 = S_f \times C^2, \quad (4)$$

where  $C$  is the dimensioned asymptotic constant in  $\text{fm}^{-1/2}$ , which connects with dimensionless AC  $C_w$  [20] by  $C = \sqrt{2k_0} C_w$ , and the dimensionless constant  $C_w$  defined from the relation [20]:

$$\chi_L(r) = \sqrt{2k_0} C_w W_{-\eta L+1/2}(2k_0 r), \quad (5)$$

where  $\chi_L(r)$  is the numerical BS radial wavefunction, obtained as the solution of the Schrödinger equation normalized to unit size,  $W_{-\eta L+1/2}(2k_0 r)$  is the Whittaker function of the bound state, determining the asymptotic behavior of the wavefunction and obtained as the solution of the same equation without nuclear potential,  $k_0$  is a wavenumber related to the channel binding energy  $E$  where  $k_0 = \sqrt{2\mu E / \hbar^2}$  in  $\text{fm}^{-1}$ ,  $\eta$  is the Coulomb parameter  $\eta = \mu Z_1 Z_2 e^2 / (\hbar^2 k_0) = 3.44476 \cdot 10^{-2} \mu Z_1 Z_2 / k_0$ ,  $Z_1$  and  $Z_2$  are the particle charges,  $L$  is the orbital momentum of the bound state.

Note that the spectroscopic factor  $S_f$  is used by us only for the standard procedure of the obtaining possible  $C_w$  range from the obtained in the experiment  $A_{NC}$  value [19,20].

**Potentials of the  $p^8\text{Li}$  interaction.** As in our previous works [17] for other nuclear systems, we use the potential of the Gaussian form with the point-like Coulomb term with the given orbital momentum  $L$  in each partial wave as the  $p^8\text{Li}$  interaction:

$$V(r, L) = -V_L \exp(-\gamma_L r^2). \quad (6)$$

The  $^4P_{3/2}$  level we consider as the ground state of  $^9\text{Be}$  in the  $p^8\text{Li}$  and such potential should correctly describe the AC for this channel. In order to extract this constant  $C$  in form (4) or  $C_w$  (5) from the available experimental data, let us consider information regarding the spectroscopic factors  $S_f$  and asymptotic normalization coefficients  $A_{NC}$ . For example, in [21], except for their own results, the authors add data of previous works. If to separate from these similar results, that is, with closely spaced values of spectroscopic factors that can be presented in the form of Table 3

Table 3. Data on spectroscopic factors  $S_f$  for the GS of  $^9\text{Be}$  in the  $p^8\text{Li}$  channel from works [9,11,21,22].  $\bar{S}_f$  is the average value on data interval.

Reaction from what $S_f$	$S_f$ for the $p^8\text{Li}_{GS}$	Ref.
$^8\text{Li}(d,n)^9\text{Be}$	0.64(21)	[21]
$^{12}\text{C}(^9\text{Be}, ^8\text{Li})^{14}\text{N}$	0.73(15)	[11]
<i>Average value</i>	<i>0.69, that is, <math>\sqrt{S_f} = 0.83</math></i>	
<i>Average value on data interval</i>	<i><math>\bar{S}_f = 0.66(22), 0.43-0.88</math> <math>\sqrt{\bar{S}_f} = 0.81(14)</math></i>	
$^9\text{Be}(^8\text{Li}, ^9\text{Be})^8\text{Li}$	1.50(28)	[22]
Potential model	1.50(27)	[9]
<i>Average value on all results</i>	<i>1.09, <math>\sqrt{S_f} = 1.05</math></i>	
<i>Data interval on all results</i>	<i><math>\bar{S}_f = 1.11(68), 0.43-1.78</math> <math>\sqrt{\bar{S}_f} = 1.05(28)</math></i>	



Furthermore, the ANC  ${}^4P_{3/2}$  GS in the  $p^8\text{Li}$  channel was given in [23], where  $A_{\text{NC}} = 10.75(12) \text{ fm}^{-1/2}$  was obtained. The constant for the  ${}^6P_{3/2}$  state is much less –  $0.25(10) \text{ fm}^{-1/2}$  [23]. Therefore, we consider here only one spin channel with  $S = 3/2$ . On the basis of expression (4) and average value on interval  $\sqrt{S_f} = 0.66(22)$  from Table 2 according works [11,21] for the AC GS, the value  $C = 13.71(2.52) \text{ fm}^{-1/2}$  was obtained, and because  $\sqrt{2k_0} = 1.307$ , so dimensionless AC (5) is equal to  $C_w = 10.49(1.93)$ . However, if to use the average value  $\sqrt{S_f}$  on all works from Table 3, equals  $1.05(28)$ , then for constant  $C$ , we obtain a wider data interval  $11.06(3.06) \text{ fm}^{-1/2}$  and  $C_w = 8.46(2.34)$ . Consequently, the possible interval of  $C_w$  values on two data groups from Table 3 is approximately from 6 (from the latest data) to 12.5 (from the previous results).

Furthermore, two options of the GS potentials with FS, which allow us to obtain the dimensionless asymptotic constant  $C_w$  in the given above limits, were obtained. The parameters of these potentials  $V_L$  and  $\gamma_L$ , and also main characteristics of the nucleus, obtained with them (binding energy  $E_b$ , asymptotic constant  $C_w$ , mass radius  $\langle R \rangle_m$  and charge radius  $\langle R \rangle_{\text{ch}}$ ) are listed in Table 4.

Table 4. GS potential parameters and main characteristics of  ${}^9\text{Be}$

N o.	$V_L$ , MeV	$\gamma_L$ , $\text{fm}^{-1}$	$E_b$ , MeV	$C_w$	$\langle R \rangle_m$ , fm	$\langle R \rangle_{\text{ch}}$ , fm
1	212.15113 5	0.17	-16.88820	10.2( 1)	2.40	2.46
2	286.17804 5	0.25	-16.88820	6.6(1)	2.36	2.38

For example, potential No. 1 has the FS and leads to the binding energy -16.88820 MeV. The definition of the calculation expressions used here for the radii is given, for example, in [17]. The above AC errors are defined by their averaging over the distance interval from 6–8 to 10–12 fm, which is the AC stabilization range. The phase shift of the elastic scattering of this potential for the GS  ${}^4P_{3/2}$  smoothly decreases down to zero and at 5.0 MeV has the value of  $\sim 330^\circ$ . Here, we consider that in the presence of two bound FS and AS, the phase shift according to generalized Levinson theorem starting from  $360^\circ$  [24]. Furthermore, another option of the GS potential that leads to a smaller AC given in Table 4.

Table 5. Options of potential parameters with FS for resonance states of nuclear and some characteristics obtained with them. In the two last columns, the experimental values listed above in Table 1 are shown.

N o.	${}^{2s+1}L_J$	$V_J$ , MeV	$\gamma_J$ , $\text{fm}^{-2}$	$E_r$ (c.m.), keV	$\Gamma_{\text{c.m.}}$ , keV	$E_r$ (c.m.), keV	$\Gamma_{\text{c.m.}}$ , keV
1.	${}^4S_{3/2}$	-5	0.1	–	–	–	–
2.	${}^4D_{3/2}$	269.24 2	0.2	1100	56	1100(30)	50(22)
3.	${}^4P_{1/2}$	66.691 21	0.07 5	87	$\sim 0.4$	87(1)	0.39(1)
4.	${}^4P_{5/2}$	34.039 9	0.04	410	203	420(7)	210(20 )

Potential No. 3 from Table 5 leads to the  ${}^4P_{1/2}$  scattering phase shift, plotted in Fig. 1 by the black solid curve, which is shown at energies up to 5.0 MeV and has the resonance at 87 keV. Scattering potential No. 4 has the phase shift  ${}^4P_{5/2}$  presented in Fig. 1 by the red dashed curve and at the considered energies has the resonance at 410 keV. Potential No. 2 leads to the  ${}^4D_{3/2}$  phase shift shown in Fig. 1 by the green solid curve. All resonance potentials have the phase shift of  $90.0^\circ(1)$  at the resonance energy and the bound FS.

**Results and discussion.** *Total cross sections, S-factor and reaction rate of radiative  ${}^8\text{Li}(p, \gamma){}^9\text{Be}$  capture.* Let us discuss calculation results of the total cross sections for the proton capture on  ${}^8\text{Li}$  and comparing them with experimental measurements from [13,14]. The summed cross section is shown in Fig. 2a by the blue solid curve; the black dashed curve shows the nonresonance capture from the  $S$  wave with potential No. 1 from Table 5 to the GS with potential No. 1 from Table 4. The green dotted curve shows cross section at the capture from

the first and the second resonances for potential No. 3 and No. 4 from Table 5. The red dashed curve shows the capture from the third resonance with potential No.2 from Table 5. The parameters of the  $S$  scattering wave without FS were determined so as correctly reproduce total cross sections in the “plateau” range, which occurs at energies of 0.5 to 7 MeV. The potential No. 1 from Table 4 is used as the GS potential that reproduces AC from [23] to the best advantage.

It should be noted that there is no second resonance at 410 keV in the available data [13]. However, it exists in spectra [16,25,26], we are taking it into account. A new resonance at 410 keV not observed in experiment [13] is clearly observed in Fig. 2a. In this experiment, at this energy, the cross section minimum is observed that is difficult to explain from the viewpoint of new data on  ${}^9\text{Be}$  spectra [16]. However, it is necessary to remember that these experimental data were obtained in sixties of the past century and were not confirmed later by more modern methods.

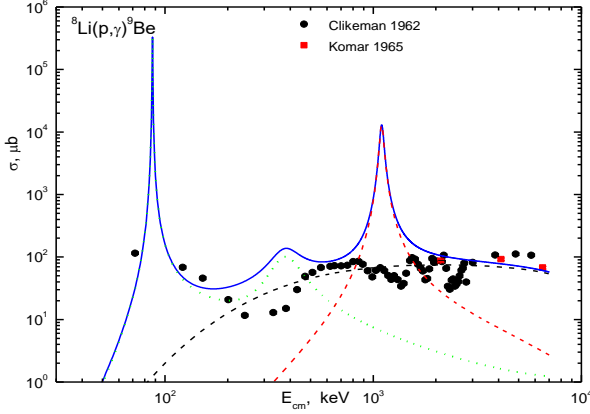


Fig. 2a Total cross sections of the radiative  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  capture to the GS of  ${}^9\text{Be}$ . Black points are experimental data from [13] and red squares are from [14]. Curves are explained in the text.

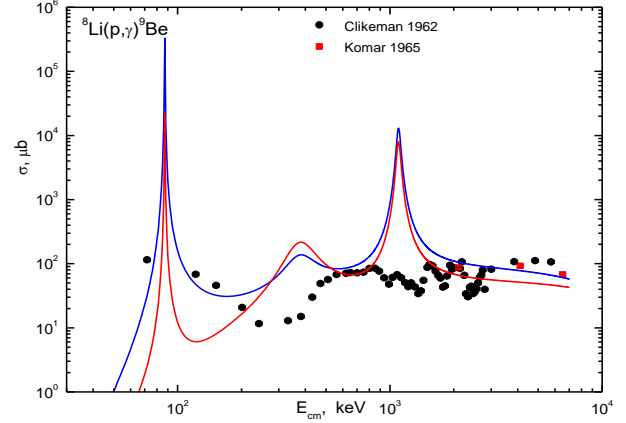


Fig. 2b Total cross sections of radiative  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  capture to the GS of  ${}^9\text{Be}$ . Notations like in Fig. 2a.

Now take note of the resonance at 1.1 MeV from Table 2, which is leading to the  $E1$  transition to the GS. The calculation results that take into account this transition are shown in Fig. 2a. The sharp rise of the total cross section is observed at the resonance energy and is shown by the red dashed curve. This resonance also is not observed in the available experimental data.

The comparison of cross sections for different GS potentials with FS is shown in Fig. 2b. The previous results for potential No. 1 from Table 4 are shown by the blue curve and the results for potential No. 2 from Table 4 are shown by the red curve. These results are slightly lower than previous ones almost in the whole energy range and overall show less agreement with the available data [13].

Now, let us discuss calculation results of the astrophysical  $S$ -factor of the radiative capture for potentials from Tables 4 and 5. They are represented in Fig. 3 – the blue curve similar to Fig. 2a, and the green dotted curve with the value of  $2.85(1)$  keV·b at 10 keV corresponds to the same curve in Fig. 2a, and black dashed curve corresponds to the same curve in Fig. 2a and shown nonresonance scattering from the  $S$  wave with the value of  $1.69(1)$  keV·b at 10 keV. The calculated  $S$ -factor at 10 keV for both options of calculations is equal to  $4.5(1)$  keV·b.

The value of  $0.15$  keV·b with a smooth decrease at  $2.0$  MeV down to  $0.1$  keV·b was obtained for the astrophysical  $S$ -factor in [21]. The interval of possible  $S$ -factor values at zero energy ( $S(0)$ ) is determined to be  $0.075$  to  $0.23$  keV·b. The value of  $0.3$  keV·b for the  $S(0)$  was obtained in [22] and furthermore up to  $1.5$  MeV the  $S$ -factor smoothly decrease approximately down to  $0.25$  keV·b. The interval of possible  $S(0)$  defined in this work near the range of  $0.21$  to  $0.38$  keV·b. In [9] the  $S(0)$  is of  $0.85$  keV·b was obtained and furthermore up to  $1.5$  MeV, the  $S$ -factor smoothly decreases approximately down to  $0.75$  keV·b. The interval of possible  $S(0)$  values defined near the range of  $0.63$  to  $1.15$  keV·b. However, in all of these works [9,21,22] none of the resonances have been taken into account and the  $S$ -factor has a smooth shape.

The general parametrization of the  $S$ -factor in the energy range up to  $50$  keV was obtained by the expression of the form:

$$S(E_{c.m.}) = S_0 + S_1E + S_2E^2, \quad (7)$$

where the energy is in keV and the corresponding parameters are  $S_0=5.082$ ,  $S_1=-0.09391$  and  $S_2=0.005359$ . For these parameters, the  $\chi^2$  value is equal to 0.26 with 5% errors comparing the initial calculated data. The result of this parametrization is shown in Fig. 3 by the red curve.

Furthermore, in Fig. 4, the green and blue solid curves show the reaction rate of the proton capture on  ${}^8\text{Li}$ , which corresponds to the same curves in Fig. 3 and is written in the form [27]:

$$N_A \langle \sigma v \rangle = 3.7313 \cdot 10^4 \mu^{-1/2} T_9^{-3/2} \int_0^\infty \sigma(E) E \exp(-11.605E/T_9) dE, \quad (8)$$

where  $E$  is in MeV, the cross section  $\sigma(E)$  is in  $\mu\text{b}$ ,  $T_9$  is the temperature in  $10^9$  K. Integration is carried out in the energy range of 10 keV–7 MeV. The black dashed curve shows the reaction rate that corresponds to the black dashed curve in Fig. 2a and takes into account only the  $E1$  transition from the  $S$  scattering wave.

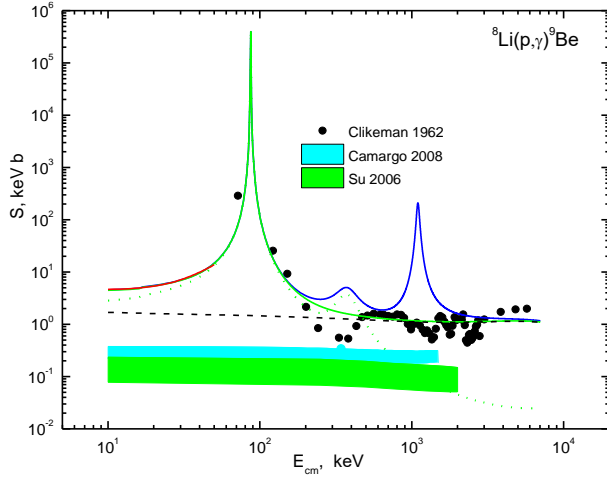


Fig. 3 Astrophysical  $S$ -factor of the radiative  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  capture to the GS of  ${}^9\text{Be}$ . Black points are experimental data from [13]. Curves are explained in the text.

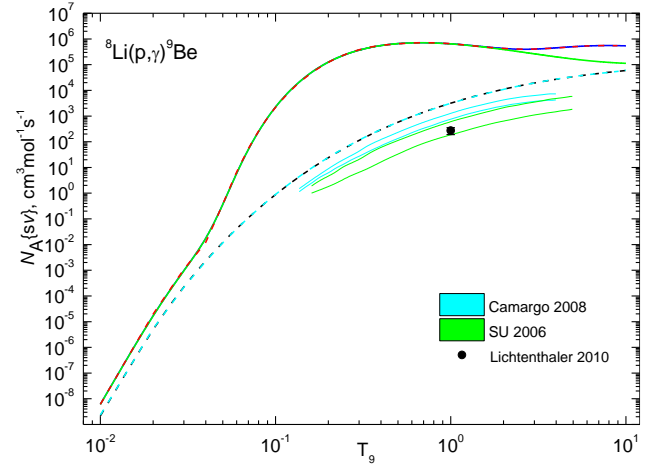


Fig. 4 Reaction rate of the proton capture on  ${}^8\text{Li}$ . Curves are explained in the text. Point is the result from [28].

Here, the reaction rate for results of paper [22] is shown by the blue band. In addition, the green band is presenting in Fig. 4 the results for the  $\langle \sigma v \rangle$  from [21]. Both of these calculations are lower than the result obtained here by some orders of magnitude. It is seen from Fig. 4 that consideration of the first resonance essentially changes the reaction rate as against results of publications [21,22], where only the nonresonance calculations were carried out. Accounting for the two next resonances in present calculations leads only to the small increasing of the  $\langle \sigma v \rangle$  at highest temperatures.

The parametrization of the reaction rate was carried out using the expression of the form [27]:

$$N_A \langle \sigma v \rangle = \frac{a_1}{T^{2/3}} \exp\left(-\frac{a_2}{T^{1/3}}\right) \left(1 + a_3 T^{1/3} + a_4 T^{2/3} + a_5 T + a_6 T^{4/3} + a_7 T^{5/3} + a_8 T^{7/3}\right) + \frac{a_9}{T^{1/2}} \exp\left(-\frac{a_{10}}{T^{1/2}}\right) + \frac{a_{11}}{T} \exp\left(-\frac{a_{12}}{T}\right) + \frac{a_{13}}{T^{3/2}} \exp\left(-\frac{a_{14}}{T^{3/2}}\right) + \frac{a_{15}}{T^2} \exp\left(-\frac{a_{16}}{T^2}\right) \quad (9)$$

with the parameters listed in Table 6. The results of these parametrization are shown above in Fig. 4 by the red dashed curve.

Table 6. Parameters of the analytical parametrization with  $\chi^2 = 0.06$  at 5% errors of the calculated total reaction rate.

$a_1$	$a_2$	$a_3$	$a_4$	$a_5$	$a_6$	$a_7$	$a_8$
-	7.52	-	5.3840	-	1095	56410	-
146.8134	023	1.57556E6	8E6	4.16671E6	16	5.0	41092.96
$a_9$	$a_{10}$	$a_{11}$	$a_{12}$	$a_{13}$	$a_{14}$	$a_{15}$	$a_{16}$
-	2.34	2.75351	0.9438	-	1.18	1.2652	0.9910
417.1643	235	E6	9	2.82805E6	361	1E6	3

**Conclusion.** It is possible to construct two-body potentials of the  $p^8\text{Li}$  interaction that allow to describe correctly the available data on characteristics of the bound state of  $^9\text{Be}$  in the  $p^8\text{Li}$  channel in the frame of the MPCM. Suggested options of the GS potentials of  $^9\text{Be}$  in the  $p^8\text{Li}$  channel allow one to obtain AC within limits of errors available for it and lead to the reasonable description of  $^9\text{Be}$  radii. Such potentials generally allow one to reproduce the available experimental data for total cross sections of the radiative proton capture on  $^8\text{Li}$  at low and ultralow energies. Obtained results for total cross sections and static characteristics of  $^9\text{Be}$  strongly depend of GS potential parameters of this nucleus in the  $p^8\text{Li}$  channel.

New results for the astrophysical  $S$ -factor and reaction rate have been obtained. They turned to be essentially higher than similar results of previous works [21,22], where the first resonance  $1/2^-$  (0.087) was not taken into account. The parametrization of the calculated  $S$ -factor in the energy range to 50 keV was carried out. Further account of two other resonances  $5/2^-$  (0.410) and  $3/2^+$  (1.100) leads only to small changes of the reaction rate at highest temperatures. Analytical parametrization of the calculated total reaction rate was carried out. As well as the nonresonance  $E1$  reaction rate was parametrized. The obtained results for the reaction rate of the proton capture on  $^8\text{Li}$  may lead to an essential re-estimation of the efficiencies of light nuclei in different thermonuclear processes in the Universe.

We consider the presented results as estimative, so as undoubtedly targeted measurements of the capture cross sections are needed in the range where our model predicts the resonance behavior of cross sections, supported by the modern data on  $^9\text{Be}$  spectra near the proton threshold. Finally, let us note that further refinement of experimental characteristics of high-lying levels of  $^9\text{Be}$  also is strongly desirable.

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## **$^8\text{Li}(p,\gamma)^9\text{Be}$ ҚАРМАУЫ КЕЗІНДЕ СӘЙКЕС $^9\text{Be}$ АСТРОФИЗИКАЛЫҚ СИНТЕЗІ ҮШІН РЕАКЦИЯ ЖЫЛДАМДЫҒЫНА РЕЗОНАНСТАРДЫҢ МӘНІ**

**Аннотация:** Юнга сызбасы бойынша орбиталық кластерлік күйді жіктеумен қатар, тыйым салынған күйдегі модификацияланған потенциалды кластерлі модель аясында, астрофизикалық энергияларда протондарды радиациялық қармауды толық кесу қарастырылған. Эксперименттік мәліметтерді алу үшін  $^9\text{Be}(\gamma,p_0)^8\text{Li}$  фотокирату реакциясын толық кесуді қайта есептеу қолданылады. Астрофизикалық энергияларда  $^8\text{Li}(p,\gamma)^9\text{Be}$  радиациялық қармау үшін гаусс потенциалдарының көрсеткіштері анықталды. Сонымен қатар, [Shoda, Tanaka (1999)]  $^9\text{Be}: ^9\text{Be}(\gamma,p)^8\text{Li}$ ,  $^9\text{Be}(\gamma,d)^7\text{Li}$ ,  $^9\text{Be}(\gamma,t)^6\text{Li}$ , сондай-ақ  $^9\text{Be}(\gamma,^3\text{He})^6\text{He}$  әртүрлі екілік тарату арналары эксперименталды зерттелді. Олардың егжей-тегжейлі тепе-теңдігімен байланысты екі бөлшекті радиациялық басып алу процестері  $^9\text{Be}$  синтезіне алып келеді және астрофизикалық қосымшалар контекстінде тиісті бағалауды талап етеді. Бұл жағдайда, бірінші үш реакция  $p^8\text{Li}$ ,  $d^7\text{Li}$  және  $t^6\text{Li}$  арналарында  $^3\text{He}^6\text{He}$ -ге қарағанда төмен кулон кедергісінің болуына, яғни 3:4 қатынасында  $^4\text{He}^5\text{He}$  арналарында, атап айтқанда 3:4 қатынасында назар аудару керек.  $^8\text{Li}(p,\gamma)^9\text{Be}$  көлденең қимасы астрофизикалық қызығушылық тудыратын энергия кезіндегі екінші  $^8\text{Li}$  шоғырдың және шағын қиманың төмен қарқындылығынан тікелей анықтау қиын. Сонымен қатар,  $^8\text{Li}(p,\gamma)^9\text{Be}$  реакциясын зерттеу мәселесі  $^8\text{Li}$ -838 мс ядросының жартылай ыдырауының өте аз кезеңінде қималарды тікелей эксперименталды өлшеу мүмкін емес болып табылады. Алайда,  $n^8\text{Li}$ -қармау жағдайында да радиациялық қармау моделін және спектроскопиялық факторды пайдалана отырып, тікелей қармау қимасын алу үшін кейбір жанама әдістер пайдаланылуы мүмкін.  $^9\text{Be}$  механизмдердің пайда болуын зерттеу  $A = 8$  массалы саңылауды еңсеру және ерте Әлемдегі ауыр элементтердің синтезіне, сонымен қатар *supernovae*  $r$ -процесс нуклеосинтез мәселесіне тікелей қатынасы бар. Қазіргі таңда  $^9\text{Be}$  екі сатылы үрдіс нәтижесінде пайда болады деген ой қалыптасты:  $\alpha(\alpha,\gamma)^8\text{Be}$  альфа бөлшектердің радиациялық қармауы қысқа ғұмырлы изотоптың  $^8\text{Be}$  ( $t_{1/2} = 6.7 \times 10^{-17}$  s) синтезіне,

одан кейін  ${}^8\text{Be}(n,\gamma){}^9\text{Be}$  нейтронының радиациялық қармауына әкеліп соғады. Бұл мақалада біз төменгі астрофизикалық энергиядағы  $p{}^8\text{Li} \rightarrow {}^9\text{Be}\gamma$  реакциясын қарастырамыз, себебі жарияланғанына 20 жыл уақыт болғанына қарамастан «тәжірибелік зеттерулер жоспары» ретінде рөл атқаратын Terasawa et al. фундаменталды жұмысындағы ауыр элементтердің синтезіне алып келетін мәнді үрдістің тізбегіне қосылған. Leistenschneider et al. (2018) жаңа жұмысында келтірілген 2 МэВ-ке дейінгі резонанс құрылымын ескере отырып 10 кэВ-тен 7.0 МэВ-ге дейінгі энергияның аймағы қарастырылған. Бұл реакцияның жылдамдығы 0.01-ден 10  $T_9$  температура аймағына ғана есептелген. Резонанстар шамалары мен орындарының реакция жылдамдығының формасы мен шамасына әсерінің анализі ұсынылған.

**Түйін сөздер:** ядролық астрофизика; бастапқы нуклеосинтез; жылулық және астрофизикалық энергиялар;  $p{}^8\text{Li}$  кластерлі жүйесі; радиациялық қармау; толық кесу.

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## ЗНАЧЕНИЕ РЕЗОНАНСОВ НА СКОРОСТЬ РЕАКЦИИ ПРИ ${}^8\text{Li}(p,\gamma){}^9\text{Be}$ ЗАХВАТЕ ДЛЯ СООТВЕТСТВУЮЩЕГО АСТРОФИЗИЧЕСКОГО СИНТЕЗА ${}^9\text{Be}$

**Аннотация:** в рамках модифицированной потенциальной кластерной модели с запрещенными состояниями, с классификацией орбитальных кластерных состояний по схемам Юнга, рассмотрены полные сечения радиационного захвата протонов на  ${}^8\text{Li}$  при астрофизических энергиях. Перерасчет полных сечений реакции фоторазвала  ${}^9\text{Be}(\gamma,p){}^8\text{Li}$  используется для получения экспериментальных данных. Были определены параметры гауссовых потенциалов для радиационного захвата  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  при астрофизических энергиях. В то же время в [Shoda, Tanaka (1999)] экспериментально исследованы различные бинарные каналы фоторасщепления  ${}^9\text{Be}$ :  ${}^9\text{Be}(\gamma,p){}^8\text{Li}$ ,  ${}^9\text{Be}(\gamma,d){}^7\text{Li}$ ,  ${}^9\text{Be}(\gamma,t){}^6\text{Li}$ , а также  ${}^9\text{Be}(\gamma,{}^3\text{He}){}^6\text{He}$ . Очевидно, что связанные с ними детальным равновесием процессы двухчастичного радиационного захвата приводят к синтезу  ${}^9\text{Be}$  и требуют соответствующей оценки в контексте астрофизических приложений. При этом следует обратить внимание на то, что первые три реакции имеют кулоновский барьер в каналах  $p{}^8\text{Li}$ ,  $d{}^7\text{Li}$  и  $t{}^6\text{Li}$  ниже, чем в  ${}^3\text{He}{}^6\text{He}$  равно как и  ${}^4\text{He}{}^5\text{He}$  каналах, а именно в соотношении 3:4. Поперечное сечение  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  трудно определить непосредственно из-за низкой интенсивности вторичного  ${}^8\text{Li}$  пучка и малого сечения при энергиях, представляющих астрофизический интерес. Кроме того, проблема изучения реакции  ${}^8\text{Li}(p,\gamma){}^9\text{Be}$  заключается еще и в том, что прямое экспериментальное измерение сечений оказывается практически невозможным из-за очень малого периода полураспада ядра  ${}^8\text{Li}$  - 838 мс. Однако, как и в случае  $n{}^8\text{Li}$ -захвата, могут быть использованы некоторые косвенные методы для извлечения сечения прямого захвата с использованием модели радиационного захвата и спектроскопического фактора. Исследование механизмов образования  ${}^9\text{Be}$  имеет прямое отношение к проблеме преодоления массовой щели с  $A = 8$  и синтезу более тяжелых элементов в ранней Вселенной, а также в  $r$ -процесс нуклеосинтеза в суперновых. В настоящее время сложилось мнение, что  ${}^9\text{Be}$  образуется в результате двухступенчатого процесса: радиационный захват альфа-частиц  $\alpha(\alpha,\gamma){}^8\text{Be}$  приводит к синтезу короткоживущего изотопа  ${}^8\text{Be}$  ( $t_{1/2} = 6.7 \times 10^{-17}$  s), и далее радиационный захват нейтрона  ${}^8\text{Be}(n,\gamma){}^9\text{Be}$ . В данной статье мы рассматриваем реакцию  $p{}^8\text{Li} \rightarrow {}^9\text{Be}\gamma$  при низких астрофизических энергиях в связи с тем, что она включена в цепочку значимых процессов, которые приводят к синтезу более тяжелых элементов в фундаментальной значимой работе Terasawa et al., которая с момента ее опубликования следующие почти 20 лет играет роль некоторого «плана практических исследований». Рассмотрена область энергий от 10 кэВ до 7.0 МэВ, но с учетом структуры резонансов только до 2 МэВ, которая была приведена в новой работе Leistenschneider et al. (2018). Скорость этой реакции рассчитана в области температур от 0.01 до 10  $T_9$ . Представлен анализ влияния положения и величины резонансов на величину и форму скорости реакции.

**Ключевые слова:** ядерная астрофизика; первичный нуклеосинтез; тепловые и астрофизические энергии; кластерная система  $p{}^8\text{Li}$ ; радиационный захват; полное сечение.

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## МАЗМҰНЫ

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